

## MASTER 1

## MARKET FINANCE

(durée 1h30)

Lundi 14 janvier 2013 ~ 10h00 -11h30

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**Exercise 1**

A person has an expected utility function of the form  $U(W) = \ln[W]$ . He initially has wealth of 4. He also has a lottery ticket that will be worth 12 with probability 0.5 and will be worth 0 (nothing) with probability 0.5.

- a) Compute the Arrow-Pratt absolute and relative risk aversion.
- b) Compute the expected utility.
- c) What is the lowest price,  $p$ , at which he would sell the ticket?
- d) Without going through the calculations how question b) would change if the person had a wealth of 10. Explain your answer.

**Exercise 2**

On the capital market two securities with the following risk-return characteristics exist:

Stock A:  $E[r_A] = 10\%$        $\sigma_A = 20\%$ Stock B:  $E[r_B] = 15\%$        $\sigma_B = 25\%$ 

- a) Assume that you own a portfolio which consists of 35% stock A and 65% stock B.
  - i. Compute the expected return and the variance of the portfolio.
  - ii. For which correlation between the stocks  $\rho_{A,B}$  is the standard deviation of the portfolio return maximal and minimal respectively.
- b) Compute the maximal and minimal standard deviation of the portfolio return.
- c) Assume that  $\rho_{A,B} = 0$ . Is it possible to realize a portfolio with  $E[r_p] = 14\%$  if the risk should maximally be  $\sigma_p = 20\%$ . For this, determine the risk for an efficient portfolio with  $E[r_p] = 14\%$ .

**Exercise 3**

Explain the main contribution of the APT, how it relates to the CAPM and the reason of its name.

**Exercise 4**

Indicate if the following statements are true or false and explain your answer.

- a) In an efficient market the expected returns of the financial assets are equal to 0.
- b) The value of a portfolio constituted by a call option and future written on the same asset and same expiry date can be negative.
- c) The future price is the price you pay to enter into a future contract.
- d) The risk free rate puzzle states that the risk free rate is too low.
- e) The prices of a strong form efficient market do not reflect private information.